

★ Draw a unit circle and label each of the quadrantal angles in degrees and in radians. Label the coordinate points at the quadrantal angles.

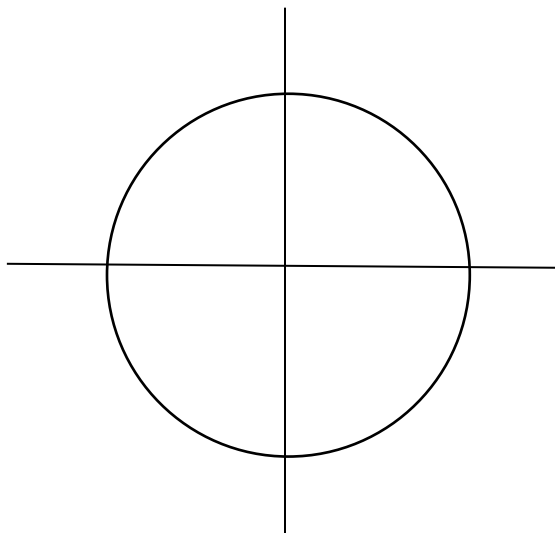
$0^\circ = \underline{\hspace{2cm}} \text{ radians}$

$90^\circ = \underline{\hspace{2cm}} \text{ radians}$

$180^\circ = \underline{\hspace{2cm}} \text{ radians}$

$270^\circ = \underline{\hspace{2cm}} \text{ radians}$

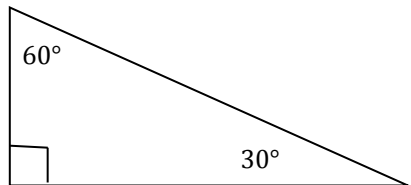
$360^\circ = \underline{\hspace{2cm}} \text{ radians}$



★ Cosine is the \_\_\_\_\_ coordinate      Sine is the \_\_\_\_\_ coordinate      Tangent is \_\_\_\_\_

★ Secant is \_\_\_\_\_      Cosecant is \_\_\_\_\_      Cotangent is \_\_\_\_\_

★ Label the sides of this  $30^\circ - 60^\circ - 90^\circ$  triangle and find the exact values of the trig functions at the right.



$\sin 30^\circ =$

$\csc 30^\circ =$

$\cos 30^\circ =$

$\sec 30^\circ =$

$\tan 30^\circ =$

$\cot 30^\circ =$

$\sin 60^\circ =$

$\csc 60^\circ =$

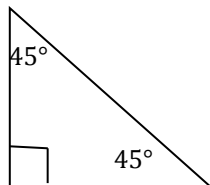
$\cos 60^\circ =$

$\sec 60^\circ =$

$\tan 60^\circ =$

$\cot 60^\circ =$

★ Label the sides of this  $45^\circ - 45^\circ - 90^\circ$  triangle and find the exact values of the trig functions at the right..



$\sin 45^\circ =$

$\csc 45^\circ =$

$\cos 45^\circ =$

$\sec 45^\circ =$

$\tan 45^\circ =$

$\cot 45^\circ =$

**Using the unit circle, find the exact value for the following without a calculator. If there is no answer possible, write "undefined."**

**1.**  $\sin 90^\circ$

**2.**  $\csc 90^\circ$

**3.**  $\cos 180^\circ$

**4.**  $\sec 180^\circ$

**1.** \_\_\_\_\_

**2.** \_\_\_\_\_

**3.** \_\_\_\_\_

**4.** \_\_\_\_\_

**5.**  $\tan 270^\circ$

**6.**  $\cot 270^\circ$

**7.**  $\sin 180^\circ$

**8.**  $\cot 180^\circ$

**5.** \_\_\_\_\_

**6.** \_\_\_\_\_

**7.** \_\_\_\_\_

**8.** \_\_\_\_\_

**9.**  $\tan 0^\circ$

**10.**  $\cos 90^\circ$

**11.**  $\sin 270^\circ$

**12.**  $\csc 360^\circ$

**9.** \_\_\_\_\_

**10.** \_\_\_\_\_

**11.** \_\_\_\_\_

**12.** \_\_\_\_\_

**13.**  $\sec \pi$

**14.**  $\cos \frac{3\pi}{2}$

**15.**  $\cot \frac{\pi}{2}$

**16.**  $\cos \pi$

**13.** \_\_\_\_\_

**14.** \_\_\_\_\_

**15.** \_\_\_\_\_

**16.** \_\_\_\_\_

**17.**  $\tan 2\pi$

**18.**  $\csc \frac{3\pi}{2}$

**19.**  $\sin \frac{3\pi}{2}$

**20.**  $\tan \frac{\pi}{2}$

**17.** \_\_\_\_\_

**18.** \_\_\_\_\_

**19.** \_\_\_\_\_

**20.** \_\_\_\_\_

**Draw the angle in standard position. Then find the reference angle.**

21.  $124^\circ$  Ref. Angle: \_\_\_\_\_

22.  $208^\circ$  Ref. Angle: \_\_\_\_\_

23.  $330^\circ$  Ref. Angle: \_\_\_\_\_

24.  $1240^\circ$  Ref. Angle: \_\_\_\_\_

25.  $1074^\circ$  Ref. Angle: \_\_\_\_\_

26.  $915^\circ$  Ref. Angle: \_\_\_\_\_

27.  $-130^\circ$  Ref. Angle: \_\_\_\_\_

28.  $-195^\circ$  Ref. Angle: \_\_\_\_\_

**Steps to find exact values of trigonometry values.**

1. Draw the angle in standard form (draw the terminal side of the angle as the HYPOTENUSE to a right triangle).
2. Find the reference angle and place it on the picture.
3. Draw a right triangle to the x-axis and fill in all the angles.
4. Label all the sides – be sure to put negative signs in front of the values of the sides that go to the left or down. They hypotenuse is **always** POSITIVE.
5. Evaluate.

***Use the reference angle to find the EXACT VALUE of each trigonometric function. Do NOT use a calculator!***

29.  $\sin 135^\circ$

30.  $\cos 120^\circ$

31.  $\tan 210^\circ$

29. \_\_\_\_\_

30. \_\_\_\_\_

31. \_\_\_\_\_

Use the reference angle to find the EXACT VALUE of each trigonometric function. Do NOT use a calculator!

32.  $\sin 240^\circ$

33.  $\tan 300^\circ$

34.  $\cos 300^\circ$

32. \_\_\_\_\_

33. \_\_\_\_\_

34. \_\_\_\_\_

35.  $\csc 60^\circ$

36.  $\sin 120^\circ$

37.  $\tan 315^\circ$

35. \_\_\_\_\_

36. \_\_\_\_\_

37. \_\_\_\_\_

38.  $\sec 120^\circ$

39.  $\cot 225^\circ$

40.  $\tan 150^\circ$

38. \_\_\_\_\_

39. \_\_\_\_\_

40. \_\_\_\_\_

41.  $\tan 240^\circ$

42.  $\cos 225^\circ$

43.  $\cos 210^\circ$

41. \_\_\_\_\_

42. \_\_\_\_\_

43. \_\_\_\_\_

***Without a calculator, find the following exact values. Use the answers from #29-43.***

**44.**  $\sec 120^\circ - \cos 120^\circ$

**44.** \_\_\_\_\_

**45.**  $\tan 315^\circ + \sin 240^\circ \cos 120^\circ$

**45.** \_\_\_\_\_

**46.**  $\tan 315^\circ + \cos 300^\circ \sec 120^\circ$

**46.** \_\_\_\_\_

**47.**  $\cot 225^\circ - \tan 315^\circ$

**47.** \_\_\_\_\_

**48.**  $\cos 225^\circ \sin 135^\circ$

**48.** \_\_\_\_\_

**49.**  $\sin 120^\circ \tan 150^\circ$

**49.** \_\_\_\_\_

**Find the exact value of each expression.**

**50.**  $\sin\theta = -\frac{\sqrt{3}}{2}$ ,  $270^\circ < \theta < 360^\circ$ ; find  $\cot\theta$

**51.**  $\cos\theta = -\frac{\sqrt{2}}{2}$ ,  $180^\circ < \theta < 270^\circ$ ; find  $\csc\theta$

**52.**  $\tan\theta = -1$ ,  $90^\circ < \theta < 180^\circ$ ; find  $\sec\theta$

**53.**  $\csc\theta = -2$ ,  $180^\circ < \theta < 270^\circ$ ; find  $\tan\theta$

**54.**  $\sin\theta = -\frac{1}{2}$  and  $\cos\theta = \frac{\sqrt{3}}{2}$ ; find  $\cot\theta$

**55.**  $\cos\theta = -\frac{\sqrt{3}}{2}$  and  $\sin\theta = -\frac{1}{2}$ ; find  $\tan\theta$

**56.**  $\csc\theta = 2$  and  $\cot\theta = -\sqrt{3}$ ; find  $\cos\theta$

**57.**  $\sec\theta = -\sqrt{2}$  and  $\sin\theta = -\frac{\sqrt{2}}{2}$ ; find  $\tan\theta$

- |               |                           |                               |                           |
|---------------|---------------------------|-------------------------------|---------------------------|
| 1. 1          | 18. $-1$                  | 34. $\frac{1}{2}$             | 49. $-\frac{1}{2}$        |
| 2. 1          | 19. $-1$                  | 35. $\frac{2\sqrt{3}}{3}$     | 50. $-\frac{\sqrt{3}}{3}$ |
| 3. $-1$       | 20. undefined             | 36. $\frac{\sqrt{3}}{2}$      | 51. $-\sqrt{2}$           |
| 4. $-1$       | 21. $56^\circ$            | 37. $-1$                      | 52. $-\sqrt{2}$           |
| 5. undefined  | 22. $28^\circ$            | 38. $-2$                      | 53. $\frac{\sqrt{3}}{3}$  |
| 6. 0          | 23. $30^\circ$            | 39. 1                         | 54. $-\sqrt{3}$           |
| 7. 0          | 24. $20^\circ$            | 40. $-\frac{\sqrt{3}}{3}$     | 55. $\frac{\sqrt{3}}{3}$  |
| 8. undefined  | 25. $6^\circ$             | 41. $\sqrt{3}$                | 56. $-\frac{\sqrt{3}}{2}$ |
| 9. 0          | 26. $15^\circ$            | 42. $-\frac{\sqrt{2}}{2}$     | 57. 1                     |
| 10. 0         | 27. $50^\circ$            | 43. $-\frac{\sqrt{3}}{2}$     |                           |
| 11. $-1$      | 28. $15^\circ$            | 44. $-1\frac{1}{2}$           |                           |
| 12. undefined | 29. $\frac{\sqrt{2}}{2}$  | 45. $\frac{-4 + \sqrt{3}}{4}$ |                           |
| 13. $-1$      | 30. $-\frac{1}{2}$        | 46. $-2$                      |                           |
| 14. 0         | 31. $\frac{\sqrt{3}}{3}$  | 47. 2                         |                           |
| 15. 0         | 32. $-\frac{\sqrt{3}}{2}$ | 48. $-\frac{1}{2}$            |                           |
| 16. $-1$      | 33. $-\sqrt{3}$           |                               |                           |
| 17. 0         |                           |                               |                           |